

EFFECT OF FISSURE DRAINAGE ON DISPERSIVE MIXING IN POROUS MEDIA GRAVITY CURRENTS: AN EXPERIMENTAL INVESTIGATION

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ABSTRACT

The prospect of storing hydrogen in depleted natural gas reservoirs requires that the dispersive mixing between injected hydrogen and the cushion gas resident within the porous medium be well understood. Motivated by this observation, we report a series of similitude laboratory experiments employing salt and fresh water; these experiments use optical techniques to characterize the dispersive mixing that results from porous media gravity current flow. Importantly, the gravity current is assumed to propagate over a "leaky" boundary, i.e. one containing an isolated fissure that allows drainage into an underlying (and dynamically-isolated) layer. Thus, we find that drainage and dispersion are connected: as more (relatively undiluted) fluid drains through the fissure, the remaining gravity current fluid is disproportionately comprised of fluid that has been significantly diluted through dispersive mixing. A novel metric for comparing the relative amount of dispersed fluid present is proposed. We then characterize the variation of this so-called dispersed buoyancy fraction with the gravity current density and source height, the dip angle and the fissure geometry. Thus dispersion increases sharply for down-dip flow whereas dispersion may plateau as the fissure area is increased. Select experimental data are contrasted against the predictions of a previously-published theoretical model. The implications of this comparison are then discussed e.g. in the context of model refinement.

KEYWORDS

Dispersion, Gravity current in porous media, Underground hydrogen storage, UHS



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1. INTRODUCTION

The quest for affordable, sustainable energy sources has intensified in recent years as the detrimental impact of atmospheric carbon emissions has become increasingly evident. Among the potential substitutes for hydrocarbon-based fuels, hydrogen stands out due to its high energy density (on a per unit mass basis) and its ability to contribute to many different components of the energy value chain – see e.g. Figure 1 of Hematpur et al. (14); see also Dunn (7). While the motivation to generate hydrogen via

electrolysis using renewable sources such as wind and solar is clear and compelling, supply inconsistencies necessitate the construction of facilities to store hydrogen for durations ranging from days to years (15). Short-term storage can be handled easily using pressurized tanks and related surface infrastructure, however, long-term storage of large volumes of hydrogen requires the injection and subsequent withdrawal of compressed gas into geological formations. Indeed, underground hydrogen storage (UHS) offers enormous storage potential, i.e. in the range of 100 GWh according to the predictions of Tarkowski (28). Realizing this potential requires exploiting various UHS facilities, including abandoned mines (4, 19), lined rock (17) or salt caverns (21, 12, 14), aquifers, (9, 25) and depleted oil and natural gas reservoirs (1, 11, 8, 18). Although salt cavern storage offers numerous benefits (e.g. a comparatively sterile environment and minimal hydrogen loss by diffusion), thick halite beds have a geographical distribution described as “limited” (14). Much more plentiful are aquifers and depleted oil and gas reservoirs and, indeed, these formations typically offer the greatest storage capacity. In either case, however, storage security may be complicated by other factors such as mixing between compressed hydrogen and “cushion gas,” the gas (e.g. CO₂ or N₂) left in formation to maintain operational pressure and to separate hydrogen from water (8, 27, 26, 3).

For hydrogen plumes that propagate laterally under the influence of buoyancy, the mixing described at the end of the last paragraph is expected to be predominately dispersive in nature. As such, Heinemann et al. (13) predicted that the mixing would be enhanced by reservoir heterogeneities. This prediction was verified and quantified by the similitude laboratory experiments of Sahu & Neufeld (24) who studied buoyancy-driven flow through a medium consisting of stacked horizontal layers of different permeability. As illustrated schematically in Figure 1 of Huppert et al. (16), flow focused through high permeability layers causes the vertical density gradient to become unstable, leading to the formation of convective fingers oriented perpendicular to the permeability jump (see also Fig. 7 of Huppert et al. (16)). Finger elongation is associated with rapid mixing in the vertical direction and a thickening of the gravity current so that it can no longer be considered long and thin.

Herein, we tackle a problem complementary to Sahu & Neufeld (24). More precisely, we return to a homogeneous porous medium but impose local rather than distributed drainage for the gravity current that propagates through this medium. In turn, drained fluid shall, after exiting the fissure, flow into a deep layer so that its subsequent flow evolution becomes disconnected from that of the original gravity current and vice-versa. Stated differently, the gravity currents examined in our work never lose their long and thin character. By experiencing localized drainage, however, their forward advance is significantly retarded and the gravity currents therefore become more susceptible to dispersive mixing. Quantifying this connection between drainage and dispersion for different source conditions, fissure areas and dip angles represents the central objective of this work. In order to realize this objective, we perform a series of similitude laboratory experiments using analog fluids, i.e. salt water as the injectate and fresh water as the ambient. Relative to real geological flows, therefore, the injectate density is larger than, rather than smaller than, that of the fluid saturating the porous medium. Such differences matter little insofar as the dynamical evolution of the flow, i.e. analogous similitude laboratory measurements would be obtained if the injectate was comparatively buoyant rather than dense. This equivalence notwithstanding, we emphasize that our study does not attempt to resolve the complicated dynamics associated with real UHS flows as neatly highlighted, for example, in Figure 2 of Heinemann et al. (13). Rather, our objective is to provide novel insights into dispersive mixing vis-à-vis “leaky” gravity current flow. In the long term, these insights may loosely inform estimates of hydrogen-cushion gas mixing (and, by extension, the economic viability of UHS projects). However, their more likely impact may be to motivate additional targeted UHS studies in the style of Feldmann et al. (8) in which dispersive mixing is considered as one of many complicating factors in characterizing the cyclic injection, spreading, drainage and recovery of hydrogen from depleted natural gas reservoirs.

The rest of the manuscript is organized as follows: in Section 2, we describe the laboratory set-up and the process applied for capturing experimental images. In Section 3, we define the key variables that are relevant to the later analysis of these experimental images. The image processing methodology is explained in Section 4 and qualitative and quantitative results are presented in Sections 5 and 6, respectively. Section 7 extends the analysis of Section 6 by comparing measuring data against the predictions of an analog theoretical model. Finally, Section 8 presents a series of conclusions for the work as a whole.

2. MATERIALS AND METHODS

2.1. Experimental set-up

Experiments were conducted under ambient conditions within a transparent acrylic tank, measuring 118 cm in length, 7.6 cm in width, and 60 cm in depth (**Fig. 1**). Relative to its bottom boundary, the tank was filled over the approximate depth range $z = 16$ cm to $z = 40$ cm with a random distribution of $3.0 \text{ mm} \pm 0.2 \text{ mm}$ diameter glass beads. After adding the beads, the tank was then filled over its entire depth with tap water of density, $\rho_a = 0.998 \text{ g/cm}^3$. According to information provided by the manufacturer, the bead density was 1.54 g/cm^3 , large enough that the bead pack did not deform under the influence of fluid flow.

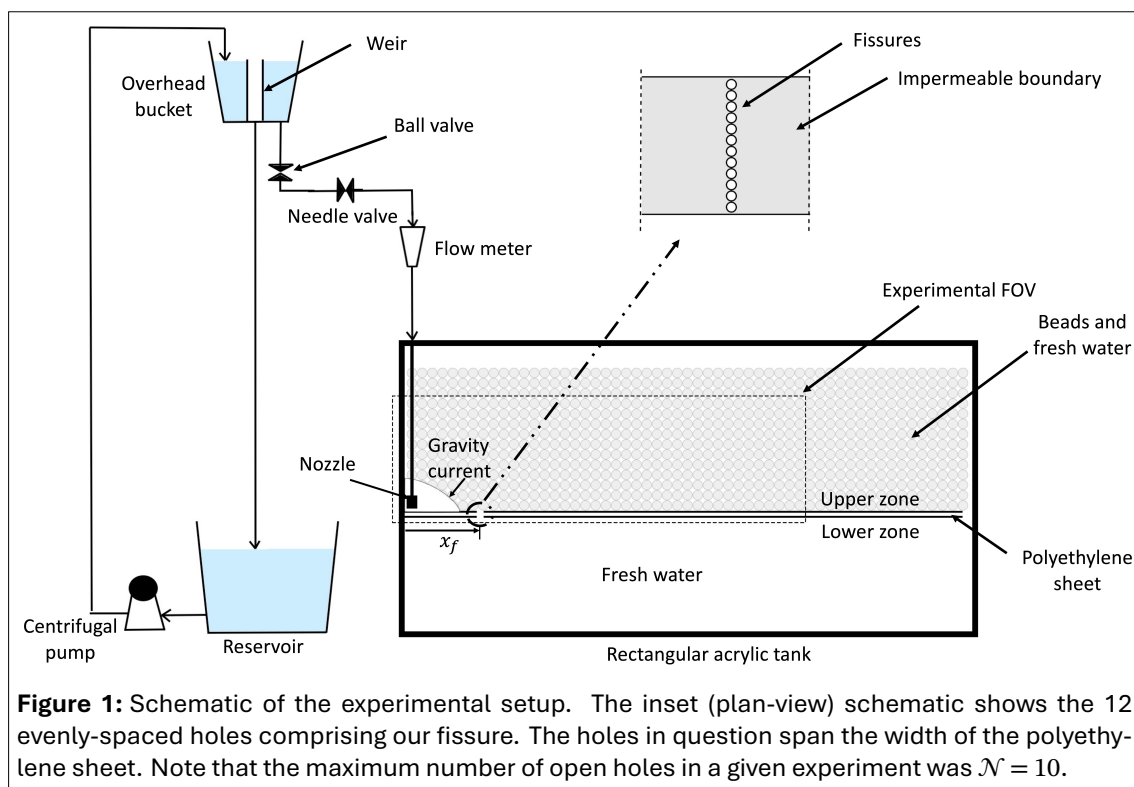
The tank was divided into upper versus lower zones using an opaque 1/4-inch polyethylene sheet that extended 115 cm longitudinally. To isolate one zone from the other and prevent unwanted leaks of dense gravity current fluid, 1/8-inch gasket tape was added to the edges of the polyethylene sheet. In turn, the polyethylene sheet was supported by five, 15 cm tall 3-D printed polyvinyl chloride (PVC) I-beams to ensure stability. The I-beam spacing and polyethylene rigidity were such that the sheet exhibited minimal deformations, i.e. the bottom boundary of the flow domain can be considered flat.

Although the polyethylene sheet and perimetric gasket formed an otherwise impermeable barrier, we drilled a total of 12 evenly-spaced holes across the sheet width where each hole diameter measured 3.175 mm – see the inset image to **Figure 1**. The openings in question were arranged in a line and were situated 15 cm from the left boundary of the tank. Meanwhile, on the right-hand side of the tank, a gap of approximately 3 cm was left between the polyethylene sheet edge and the inside tank wall. This gap, which was covered with a stiff mesh to prevent a collapse of the bead pack, provided a passageway for ambient fluid to flow from the lower zone to the upper zone. Such a flow was a necessary consequence of drainage through the fissure, i.e. the 3 cm gap insured that the fissure flow was unidirectional and downward. In turn, drainage was unimpeded by obstacles to the flow path from the lower zone because the lower zone was devoid of glass beads. In the upper zone, by contrast, the bead layer was approximately 24 cm thick. We estimated the medium permeability, k , using the semi-empirical relationship proposed by Kozeny and Carman and further described by Dullien (6), i.e.

$$k = \frac{d^2 \phi^3}{180(1 - \phi)^2} \quad (1)$$

Here d is the bead diameter and ϕ is the porosity. Consistent with the random packing arrangement of the (spherical) glass beads, we set $\phi = 0.38$ (10).

As illustrated schematically in **Figure 1**, dense gravity current fluid was injected into the tank using a 3-D printed nozzle, which was situated in the left-most corner of the upper zone. Depending on the specific experimental setup, the nozzle was either aligned flush with the impermeable boundary, as shown in **Figure 1**, or elevated. In this latter configuration, injected fluid fell some nontrivial vertical distance before striking the polyethylene sheet, thereby accelerating and entraining ambient fluid during its descent. The nozzle discharge area measured 2.8 cm^2 , and its length measured 6.45 cm such that it very nearly spanned the inside width of the tank. Moreover, and as described in more detail in Roes (22), the nozzle was designed to minimize the source momentum flux and to discharge a uniform flow along its length, even at low flow rates. Nozzle source fluid (i.e. the injectate) consisted of a saline solution to which Procion



MX Navy dye^a was added for flow visualization purposes. In a typical experiment, the dye concentration measured 0.04 g per 1 L of tap water where the mass of dye powder was measured using an SLF303 balance^b. At such small concentrations, the dye had a negligible impact on the solution density, which was instead fixed by the addition of crystalline salt (NaCl). Solution densities were measured using a refractometer^c programmed to output fluid density based on an internal measurement of the index of refraction for salt water.

Saline fluid was supplied to the nozzle using the set-up illustrated schematically on the left-hand side of **Figure 1**. Dyed, saltwater solutions were made in 22 L batches in the floor-level reservoir. By connecting this reservoir to a centrifugal pump^d, saline fluid was added to an overhead bucket containing an internal cylindrical weir. This weir maintained a constant water level (and therefore constant nozzle supply pressure) over the course of a particular experiment. As shown in **Figure 1**, saline fluid flowing over the weir was returned to the reservoir whereas a separate saline fluid stream flowed to the nozzle and was thereafter discharged in the form of a dense gravity current. Along the way, this latter stream of saline fluid flowed through plastic tubing (inner diameter of 12.7 mm) that connected the overhead bucket to a plastic on/off ball valve^e, a flow control needle valve^e and an analog flow meter^f. Using this set-up, saline fluid flow rates of 1.0 mL/s were obtained.

2.2. Image capture and dispersion analysis

Over the course of each experiment, digital images were captured every 30 s using a digital single-lens reflex (DSLR) camera^g, outfitted with an 18-55 mm IS II zoom lens. The camera featured 5184×3156 pixels and a resolution of 72 dpi. To ensure consistent backlighting, two overhead projectors^h were used,

^aProcion MX Navy dye, Jacquard Products, USA.

^bSLF303 balance, Thermo Fisher Scientific, USA.

^cAbbemat 3000 refractometer (Anton Paar GmbH, Graz, Austria), see product documentation: [Anton Paar datasheet](#).

^dLittle Giant Pump Co., Model 3-MD, see product details: [Little Giant 3-MD series](#).

^eSwagelok, Model SS-8GUF8, see product details: [Swagelok SS-8GUF8](#).

^fGilmont Instruments, Model GV-2119-S-P, USA

^gCanon EOS Rebel T2i, 18.0 MP, see product details: [Canon EOS Rebel T2i](#).

^h3M Model 1880 overhead projectors, see product datasheet: [3M 1880 datasheet](#).

both of which were positioned at the vertical midpoint of the tank. One projector was situated between the left tank wall and the vertical mid-plane; the other was situated between the vertical mid-plane and the right tank wall. Both projectors sat 1 m behind the back wall of the tank. Along the outside surface of this back wall, we applied a sheet of tracing paper, which diffused the incoming light and thereby improved both lighting uniformity and image clarity.

It is important to reiterate that our tank width was small and the nozzle supplying dense fluid spanned almost the entire inside width. The resulting flow was therefore approximately 2-D rectilinear. Surely the flow included transverse dispersion, however, by positioning the camera directly in front of the tank, we did not visualize nor measure dispersive mixing across the tank width. Instead, and consistent with e.g. Sahu & Neufeld (24), our focus was on dispersion in the longitudinal (x) and wall-normal (z) directions. In both cases, dispersion may have been locally enhanced at the sidewalls, i.e. due to the well-known increase of porosity at a (vertical) boundary. However, and because our optical method effectively integrated dye concentrations across the entire tank width, sidewall effects were considered to be small.

2.3. Experimental sequence

As summarized in **Appendix A (Supplementary Material, available online)**, our investigation consisted of a total of 48 experiments where we varied the tank angle of inclination, θ , the number, $\mathcal{N}$, of open holes within the fissure, the source fluid density (as characterized by an Atwood number, At – see **Equation 6** below) and the nozzle elevation, z_n . Regarding the former parameter, we considered a total of five inclination angles, i.e. $\theta = -5^\circ, -2.5^\circ, 0^\circ, 2.5^\circ$ and 5° , where $\theta < 0^\circ$ and $\theta > 0^\circ$ respectively correspond to up-dip and down-dip gravity current flow. Of these five inclination angles, $\theta = 0^\circ$ proved the most temperamental owing to the difficulty of removing air bubbles from the vicinity of the fissure holes. Because of the impact of such bubbles on injectate drainage, our study of the $\theta = 0^\circ$ case was limited to scenarios where $\mathcal{N} = 0$. For other inclination angles, a greater range of $\mathcal{N}$ was possible, i.e. we considered six different fissure configurations ranging from zero fissure holes open to 10 fissure holes open. We also considered two different source fluid densities, i.e. $\rho_s \simeq 1.01 \text{ g/cm}^3$ and $\rho_s \simeq 1.02 \text{ g/cm}^3$. Finally, we considered nozzle elevations of between 0 cm (signifying a nozzle that abutted the polyethylene sheet) and 10 cm (signifying a nozzle situated at the approximate mid-depth of the bead pack and still oriented normal to the polyethylene sheet).

Underpinning each of our experiments was a series of calibration images, which were collected every time the bead pack and/or inclination angle was changed. These calibration images applied Procion MX Navy dye concentrations measuring 0%, 20%, 40%, 50%, 60%, 80%, 100%, and 120% of the dye concentration of the nozzle source fluid, i.e. the fluid contained within the reservoir of **Figure 1**. The calibration images facilitated the analysis of our experimental snapshots in a manner to be explained in Section 4. Before turning to this discussion, it is first necessary to list and discuss some of the key variables germane to our study. Such is the purpose of the following section.

3. PARAMETER CHARACTERIZATION

Consistent with Neufeld et al. (20), we define characteristic horizontal and vertical length scales as:

$$L = x_f \quad \text{and} \quad H = \left(\frac{x_f \dot{Q}_s \phi \nu}{kg'_s w} \right)^{\frac{1}{2}} \quad (2)$$

respectively, and a characteristic timescale as:

$$T = \left(\frac{x_f^3 \phi \nu w}{kg'_s \dot{Q}_s} \right)^{1/2} \quad (3)$$

In **Equation 2** and **Equation 3**, x_f is the distance from the upstream inside tank wall to the middle of the fissure – see **Figure 1**.

Also, $\dot{Q}_s$ is the source volume flow rate, ν is the water kinematic viscosity, w is the tank width, and g'_s is the reduced gravity, defined in terms of the source and ambient fluid densities as

$$g'_s = g \left(\frac{\rho_s - \rho_a}{\rho_a} \right) \quad (4)$$

Having defined the characteristic length and time scales, we can now non-dimensionalize distances and time via

$$x^* = x/L, \quad z^* = z/H, \quad t^* = t/T \quad (5)$$

The densities ρ_s and ρ_a are necessary for defining the reduced gravity g'_s of **Equation 4**; they are likewise important in defining an Atwood number, which characterizes the importance of buoyancy. The Atwood number in question is defined as

$$At = \frac{\rho_s - \rho_a}{\rho_s + \rho_a} \quad (6)$$

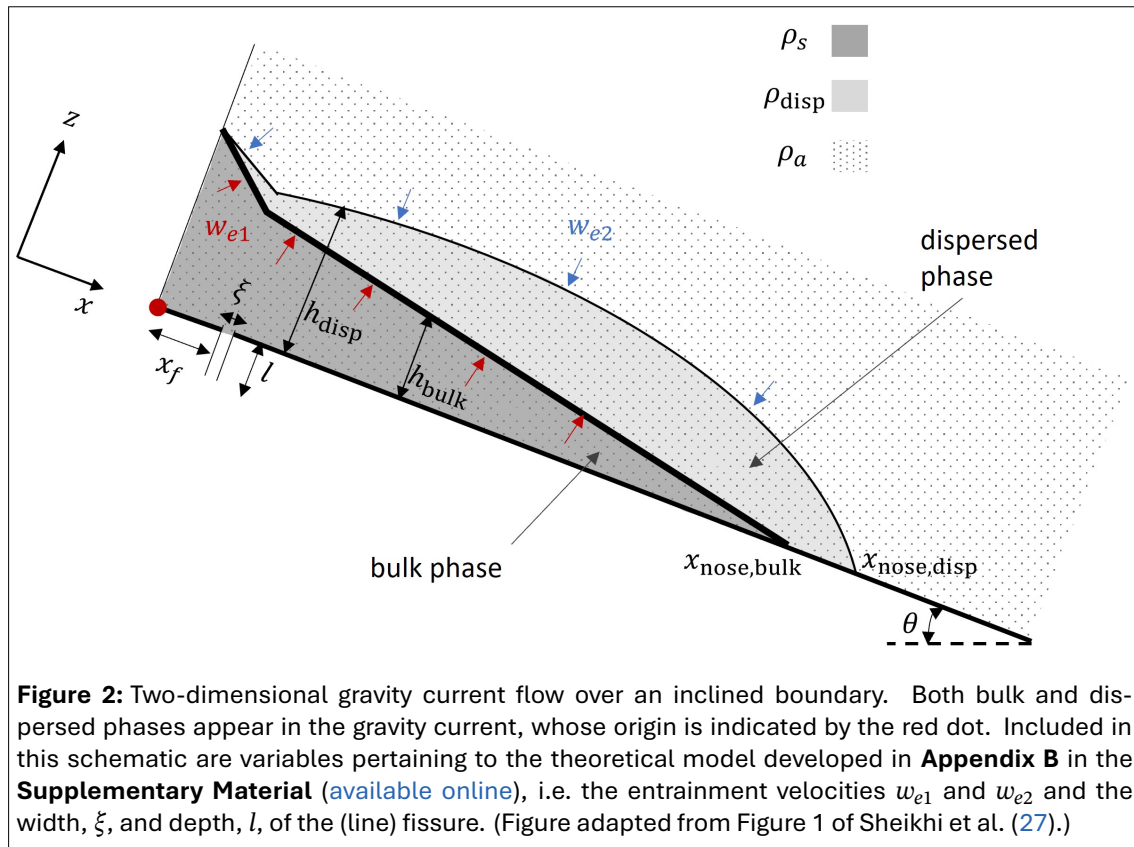
A major thrust of our investigation is to estimate, as a function of time, the amount of injected fluid that remains within, versus drains out of, the porous medium. However, characterizing this amount is subject to context. One approach is to measure the amount of fluid remaining within the porous medium by its volume. Given the approximately 2D nature of the gravity current flow in our narrow tank, we measure this volume on a per unit tank span basis. As such, and by applying the post-processing algorithms to be discussed in the next section, we calculate the resulting area using one of the following two equations:

$$A_{\text{bulk}} = \int_0^{x_{\text{nose, bulk}}} \int_0^{h_{\text{bulk}}(x)} dz dx \quad (7)$$

and

$$A_{\text{disp}} = \int_0^{x_{\text{nose, disp}}} \int_{h_{\text{bulk}}(x)}^{h_{\text{disp}}(x)} dz dx \quad (8)$$

where the dimensional (and time-dependent) variables $x_{\text{nose, bulk}}$, $x_{\text{nose, disp}}$, h_{bulk} and h_{disp} are defined in **Figure 2**. Consistent with Bharath et al. (2) and follow-on investigations, **Equation 7** and **Equation 8** distinguish between the bulk and dispersed phases of the gravity current. As we discuss in greater detail below, bulk fluid has a density comparable to ρ_s , i.e. it remains relatively undiluted by ambient fluid. Conversely, dispersed fluid has a density closer to ρ_a and so is more impacted by dispersive mixing. From **Equation 7**, A_{bulk} is the area occupied by bulk fluid and is calculated with reference to the depth, h_{bulk} , of bulk fluid measured from the neighborhood of the nozzle to the leading edge (or nose) of the bulk phase where, by definition, $h_{\text{bulk}} \rightarrow 0$. Similar comments apply to A_{disp} , which represents the area occupied by the dispersed phase. In evaluating A_{disp} from **Equation 8**, note that dispersed fluid always separates bulk fluid from ambient fluid such that $x_{\text{nose, disp}} > x_{\text{nose, bulk}}$ and $h_{\text{disp}} > h_{\text{bulk}}$. As shown in **Figure 2**, h_{disp} is the combined depth of the bulk and dispersed phases. Note, furthermore, that the nose positions $x_{\text{nose, bulk}}$ and $x_{\text{nose, disp}}$ are both measured from the upstream interior wall of the tank.



Finally, the areas defined by **Equation 7** and **Equation 8** may be rendered non-dimensional via

$$A_j^* = \frac{\phi A_j w}{\dot{Q}_s T} \quad (9)$$

where the subscript j stands for 'bulk' or 'disp.'

In other contexts, it may be more appropriate to measure the amount of source fluid remaining within the porous medium not by its volume per unit span but rather by its buoyancy per unit span, B . By this metric, the key parameters characterizing the bulk- and dispersed-phases are

$$B_{\text{bulk}} = \int_0^{x_{\text{nose,bulk}}} \int_0^{h_{\text{bulk}}(x)} g' dz dx \quad (10)$$

and

$$B_{\text{disp}} = \int_0^{x_{\text{nose,disp}}} \int_{h_{\text{bulk}}(x)}^{h_{\text{disp}}(x)} g' dz dx \quad (11)$$

respectively. Analogous to **Equation 4**, $g' \equiv g(\rho - \rho_a)/\rho_a$ where $\rho = \rho(x, t)$ is the fluid density as measured anywhere within the domain. Note, however, that outside of the bulk or dispersed phases, $\rho = \rho_a$ and $B_j = 0$. Also, and similar to **Equation 9**, we can non-dimensionalize the above variables by defining

$$B_j^* = \frac{\phi B_j w}{\dot{Q}_s g'_s T} \quad (12)$$

In the analysis to follow, we emphasize measures of buoyancy (i.e. B_{bulk} and B_{disp}) rather than of volume (i.e. A_{bulk} and A_{disp}). Consider, for instance, a scenario in which the mixing of bulk fluid results in a dispersed phase that is voluminous but dilute. A_{disp} may equal or even exceed A_{bulk} , however, a comparison of A_{disp} and A_{bulk} is misleading because most of the solute (i.e. salt and dye) remains in the bulk phase.

Comparing B_{disp} and B_{bulk} avoids this confusion because B_{disp} takes into account both the volume occupied by the dispersed fluid and also its solute concentration. By analogy with the UHS example discussed in Section 1, losing a proportion of injected hydrogen to dispersive mixing is expected. Of key importance, commercial and otherwise, is whether this fraction is large or small, not whether the gas lost spans a large or small volume within the depleted reservoir.

Motivated by the above discussion, we recognize that the fraction of the total buoyancy that resides in the dispersed phase provides a straightforward means of characterizing the degree of mixing associated with the advance and drainage of the gravity current. The quantity in question can be defined as

$$\bar{B}_{\text{disp}}^* = \frac{B_{\text{disp}}}{B_{\text{disp}} + B_{\text{bulk}}} \quad (13)$$

For brevity, we refer to $\bar{B}_{\text{disp}}^*$ as the ‘dispersed buoyancy fraction’.

4. IMAGE PROCESSING

This section outlines the crucial steps taken to distill experimental snapshots into matrices amenable to the analysis to appear in Sections 5 and 6. Each of the image processing steps was performed using Matlab.

4.1. Image alignment and conversion

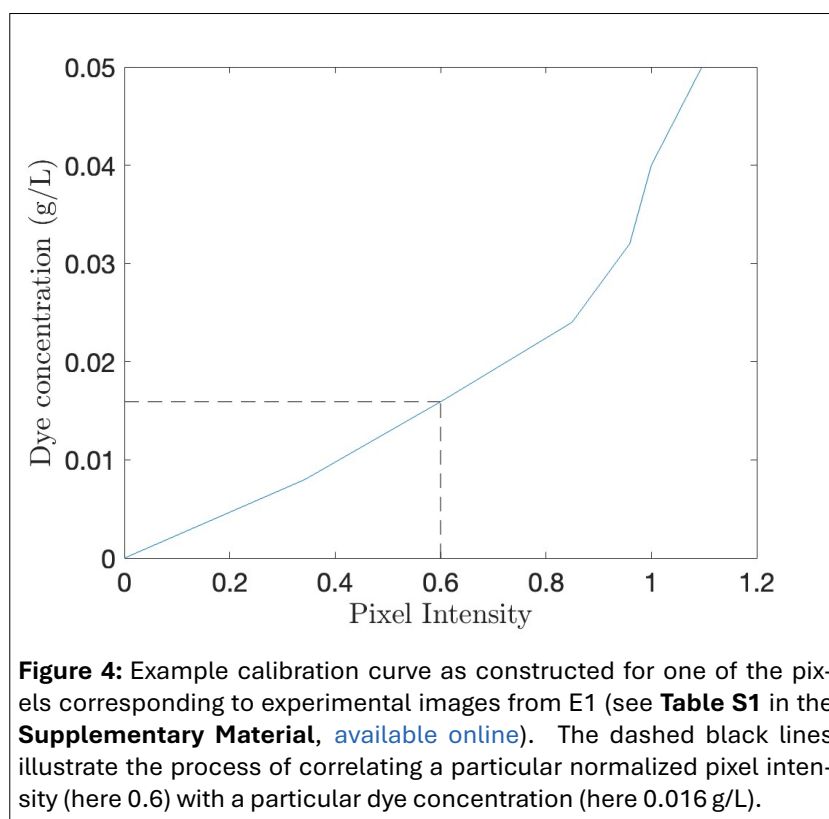
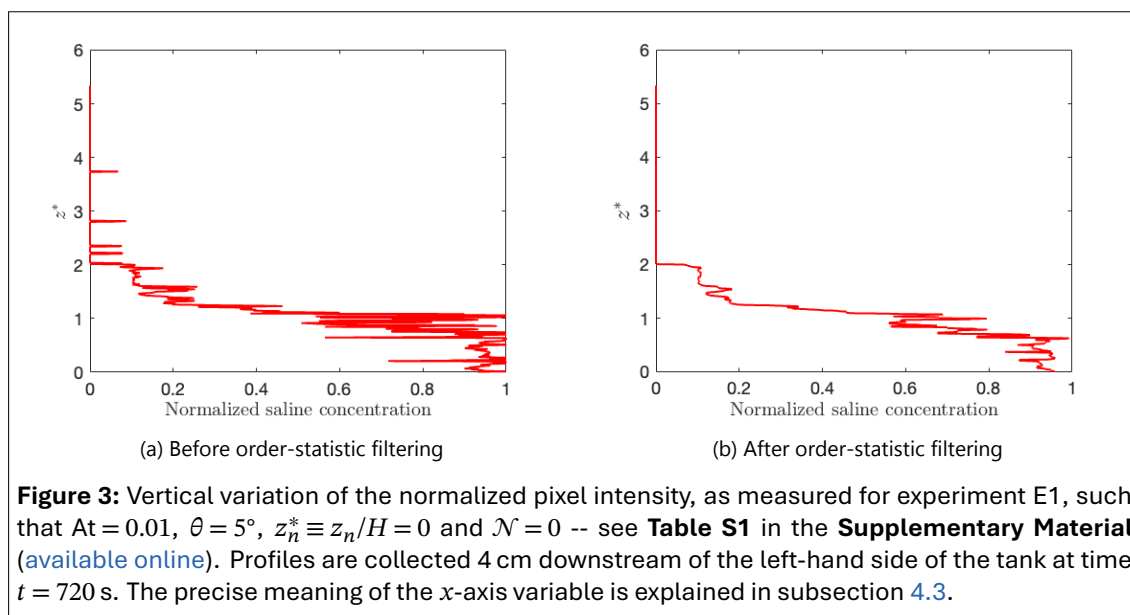
As indicated by **Table S1** in the **Supplementary Material** ([available online](#)), the vast majority of our experiments inclined the tank through a nonzero angle, θ . Because the camera orientation was fixed and parallel to the ground, images were rotated until the (perpendicular) tank edges appeared as vertical and horizontal in the Matlab figure window. RGB images were then converted to grayscale. Attention then shifted to the region of interest, specifically the area within 15 cm of the polyethylene sheet and 65 cm of the left (upstream) tank wall. However, and due to the presence of the nozzle and its 12.7 mm diameter feeder tubing, the left-most 5 cm of this rectangular region was later cropped. By applying background image subtraction (using the first image from each set, which shows the bead pack before flow initialization, as the reference), it became easier to visualize field-of-view changes resulting from the forward advance and mixing of the gravity current.

4.2. Image refinement and noise reduction

Given the sensitivity of the experiments for instance to light intensity variations, further image refinement was applied, such as using order-statistic filtering. This process helped to eliminate noise and produce a sharper gradient, enhancing the visual signatures of mixing in each of the false color (i.e. background-subtracted) images. The specific median filter applied operated over a 5×5 pixel area, identifying and replacing low-intensity areas in both calibration and experimental images with the median value of the region in question. By aligning the intensity of a particular pixel with its neighbors, this technique significantly reduced noise, for instance due to light reflection effects. Noise-reduction benefits were apparent both in regions within and outside of the gravity current. In the interests of consistency, we applied the same filtering techniques to all eight calibration images and likewise to each of the experimental images associated with that calibration set. **Figure 3** shows the variation of pixel intensity as measured from the top to bottom of a representative experimental image. The noise is substantially reduced in the right-hand side panel, which corresponds to a filtered experimental image.

4.3. Image Calibration (pixel intensity to fluid density)

Within any one of our experimental images, the process of converting pixel intensities to dye concentrations required adherence to a computationally-intensive calibration process. As noted already, each experimental image was analyzed with reference to a series of eight calibration images collected prior to flow initialization. Calibration images were captured over a range of dye intensities (see subsection 2.3)



so that at each of the more than two million pixels in a representative experimental image, an eight-point calibration curve of pixel intensity versus dye intensity could be drawn. An example of such a calibration curve is shown in **Figure 4** where pixel intensities have been normalized such that an intensity value of unity corresponds to a Procion MX Navy dye concentration of 0.04 g/L. By applying Matlab's `interp1` and linearly interpolating between the eight points comprising each calibration curve, it was possible, when analyzing laboratory images, to assign a unique dye intensity to each pixel and for every frame within an experimental data set. As with the study of Dong & Salvadurai (5), spatial variations in the bead pack intensity made it essential to construct pixel-specific calibration curves rather than, say, a universal calibration curve to be applied over the entirety of the field of view (FOV).

Of course, dye intensities are of much less interest than, say, fluid densities or solute concentrations. To this end, we exploit the fact that ours is a comparatively large-Péclet number flow such that dye and salt are expected to mix at approximately equal rates. Stated differently, a key assumption of our study is that the dye intensity serves as a direct proxy for the saline concentration. Thus can we straightforwardly convert from a normalized dye concentration to a normalized salt concentration where, consistent with the above discussion, a normalized pixel intensity of unity corresponds to a dye concentration of 0.04 g/L, which corresponds, in turn, to a normalized saline concentration of unity. Indeed, it is this latter variable that we consider in **Figure 3**. In **Figure 3**, the normalized saline concentration approaches unity towards the bottom of the field of view where gravity current densities most closely match the source density, ρ_s . Above this region of highly concentrated (or 'bulk') fluid is a dispersed region where normalized saline concentrations fall well above zero but well below unity. Characterizing the relative volume and buoyancy of this quantity of dispersed fluid is, of course, a major objective of the present study. Before turning to this topic, however, it is first necessary to distinguish between the bulk and dispersed phases. We discuss this (and other) topics next.

5. QUALITATIVE ANALYSIS

By applying the post-processing steps detailed in subsections 4.1 to 4.3, it was possible to generate images such as those presented in the collage of **Figure 5**. Here, we show snapshots collected at three different instants in time corresponding to $t^* = 0.9$ (left column), $t^* = 1.8$ (center column) and $t^* = 2.6$ (right column) where t^* is defined by **Equation 5**. This trio of images is reproduced six times over where, scanning down the columns of **Figure 5**, the number, $\mathcal{N}$, of open fissure holes increases from zero to 10 in steps of two. All other parameters (i.e. source conditions and angle of inclination) are held fixed such that $At = 0.01$, $\theta = 5^\circ$ and $z_n^* \equiv z_n/H = 0$. A figure analogous to **Figure 5**, but considering a larger source density, i.e. $At = 0.02$ is shown in **Figure 6**.

As noted in the caption to **Figure 5**, the color coding delineates the degree of dispersion realized in each experimental image. Thus, white shading appears close to the bottom of the frame in the different panels of **Figure 5** and **Figure 6**: immediately above the polyethylene sheet there is limited opportunity for diluting gravity current fluid with ambient fluid – see **Figure 3** and the discussion thereof. Above this white region, one observes shades of red, yellow, blue and black corresponding to a progression from fluid whose salinity is relatively close to that of the source versus that of the ambient.

An interesting aspect of **Figure 5** is that increasing $\mathcal{N}$ from zero to 10 has only a modest impact on the thickness of the red, yellow and blue regions. However, changing $\mathcal{N}$ has a substantial impact on the volume of fluid draining through the fissure. For instance, when $\mathcal{N} \geq 6$, the white region becomes very small even for t^* as large as 2.6. Correspondingly, and compared to the $\mathcal{N} = 0$ baseline, the gravity current advances much more slowly for large $\mathcal{N}$ with fluid having a density close to that of the source propagating little past $x^* = 1$.

Of course, a slower rate of frontal advance should not be confused with an absence of downstream influence: given sufficient time, gravity current fluid can propagate long down-dip distances, even if $\mathcal{N}$ is comparatively large. This fact is confirmed by **Figure 7**. It considers the same six experiments from **Figure 5** but shows, as a function of $\mathcal{N}$, the gravity current profile at $t_{x^*=4}$, defined as the point in time where the gravity current front first reaches the downstream location $x^* = 4$. **Figure 7** makes clear that the volume of fluid whose saline concentration falls well below ρ_s is, relative to the total volume of gravity current fluid present, substantially larger when $\mathcal{N} = 10$ versus $\mathcal{N} = 0$. Such is the consequence of having most of the high-density source fluid drain away through the open fissure. In this way, and measured in proportional rather than absolute amounts, draining and dispersion are closely linked with the former serving to increase the relative importance of the latter – c.f. Sheikhi et al. (27) and Sheikhi & Flynn (26).

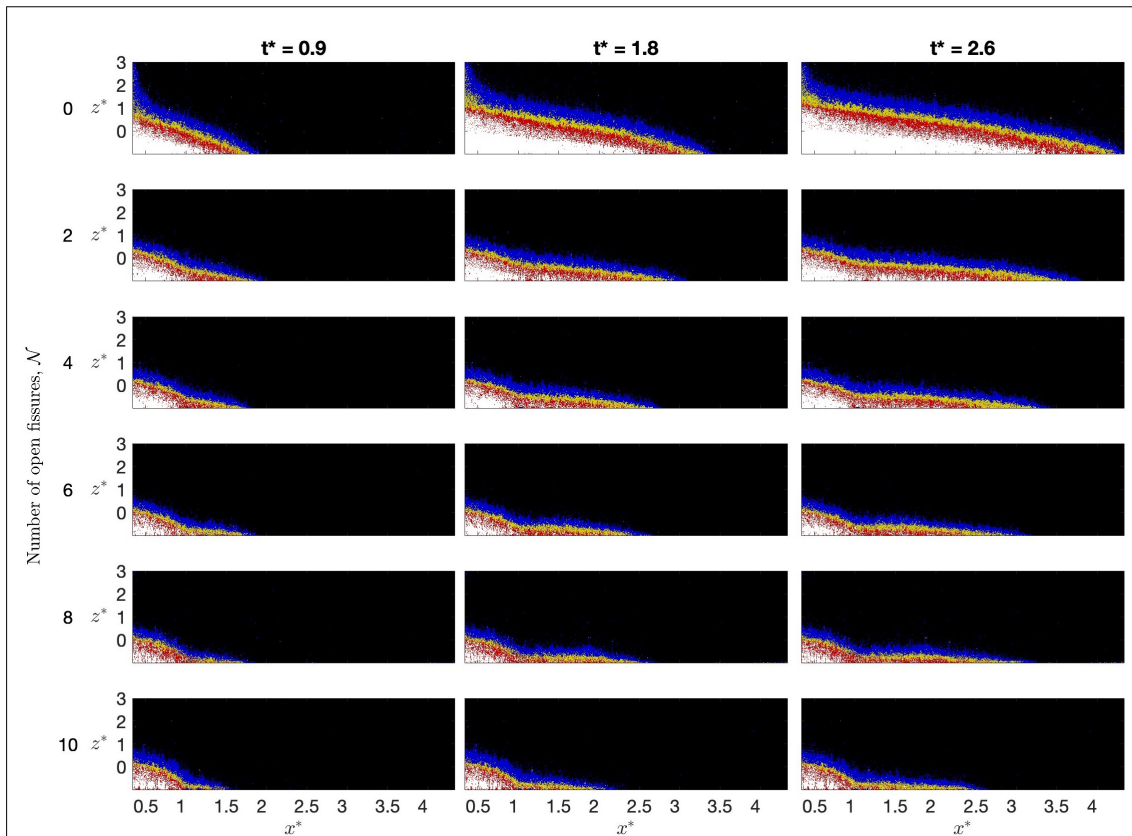


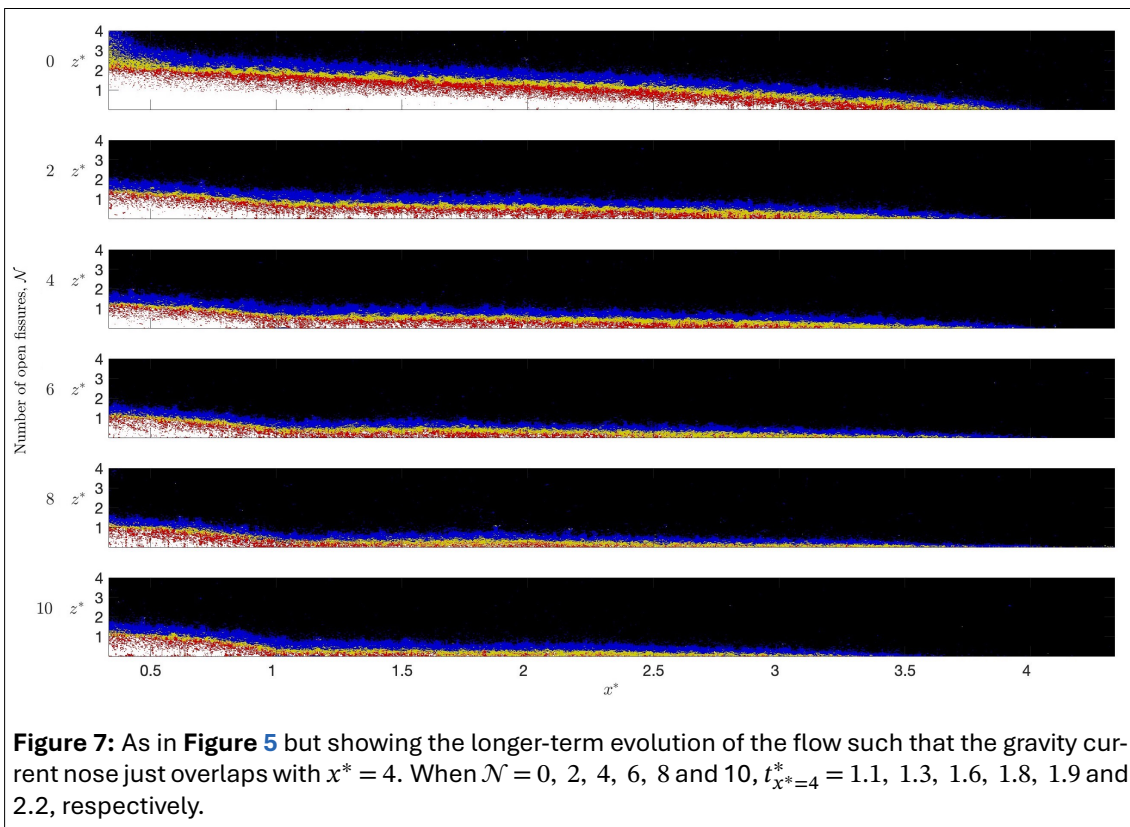
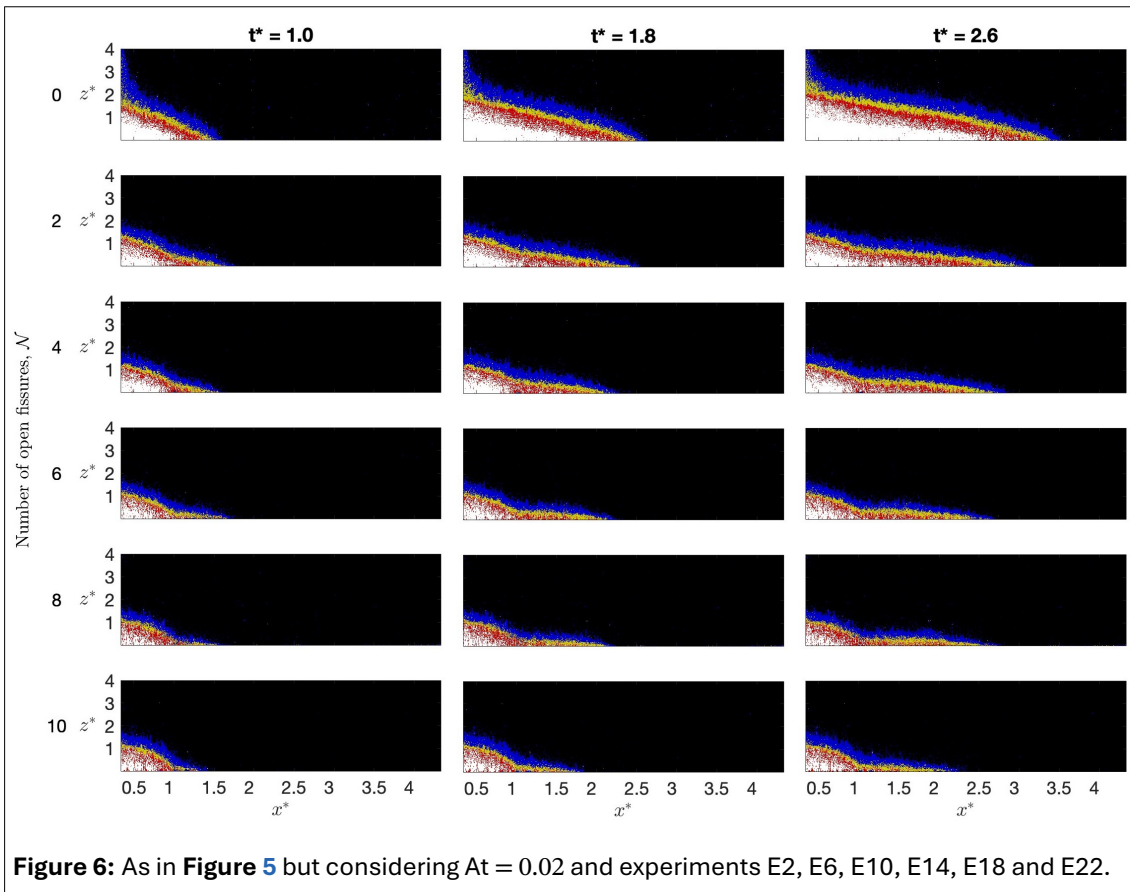
Figure 5: Collage image showing the time evolution of six different experiments (i.e. E1, E5, E9, E13, E17 and E21), each corresponding to a different number of open fissure holes. The spatial coordinates x^* and z^* are defined by **Equation 5** where $x^* = 1$ shows the fissure location. Colored shading is applied over the following range of normalized saline concentrations: black -- 0 to 0.10; blue -- 0.10 to 0.25; yellow -- 0.25 to 0.50; red -- 0.50 to 0.75; and white -- 0.75 to 1.

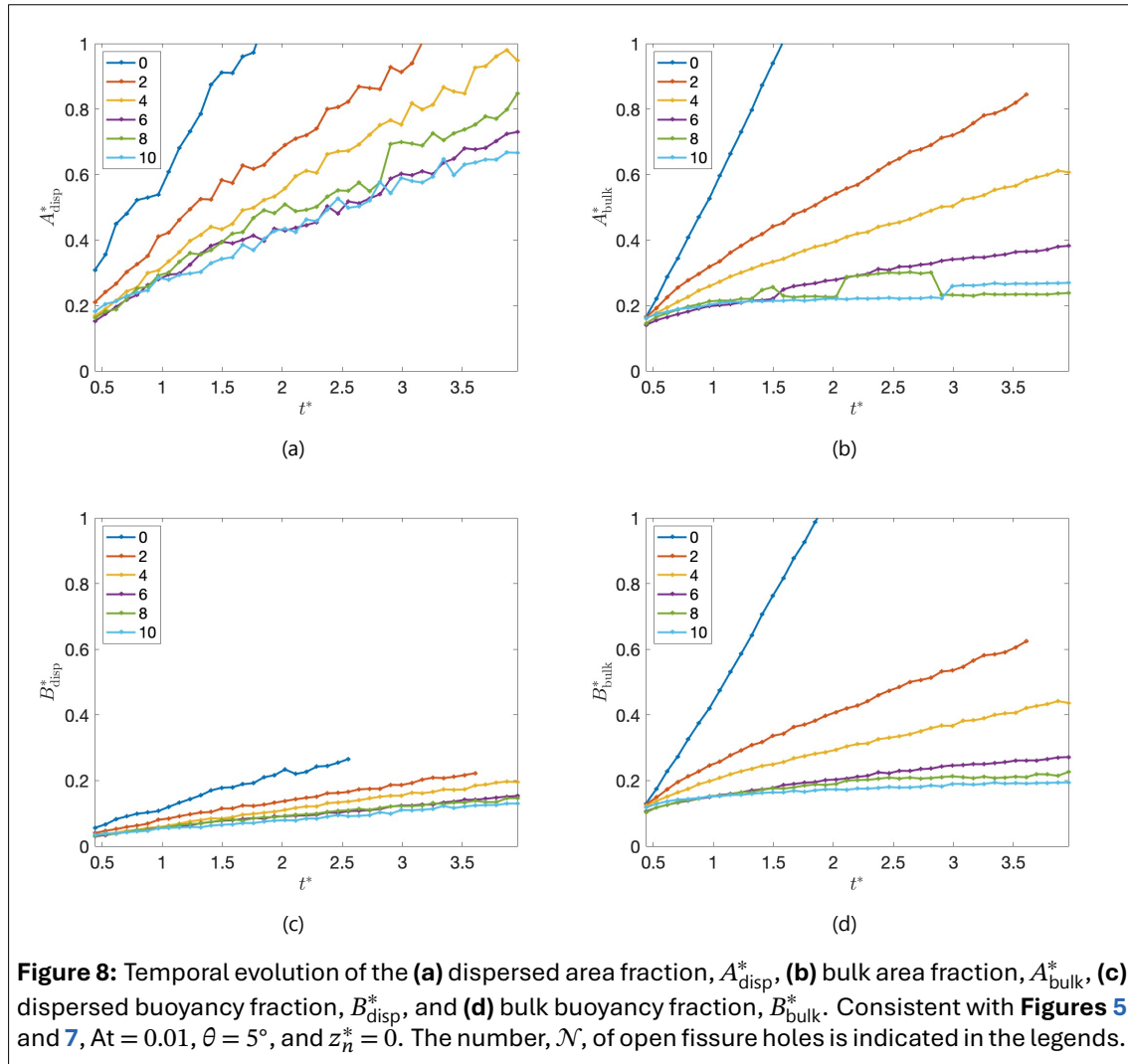
Given the conclusions from the end of the last paragraph, it is interesting to revisit the differences between **Figure 5** ($At = 0.01$) and **Figure 6** ($At = 0.02$). When the Atwood number is doubled, draining becomes even more significant such that the gravity currents of **Figure 6** advance more slowly than their counterparts from **Figure 5**. For $N \geq 4$, for instance, the region beyond the fissure is practically devoid of fluid having a normalized saline concentration exceeding 0.75. When draining is especially robust, we lack a sufficient supply of dense gravity current fluid to drive mixing by dispersion. In such large N cases, the relative significance of the yellow and blue regions will actually be shown to decrease – see e.g. **Figure 12a** below.

Notwithstanding the colorful variety of concentrations evident in **Figures 5, 6** and **7**, it is more advantageous to now transition to a binary point-of-view where we classify fluid nontrivially contaminated with salt/dye into one of two different categories. Specifically, ‘bulk’ and ‘dispersed’ fluid will respectively correspond to any fluid having a normalized saline concentration greater than and less than 0.5. In essence, bulk fluid appears as white and red in **Figures 5, 6** and **7**, whereas dispersed fluid appears as yellow and blue. Having established these definitions, we are now well positioned to examine the relative abundance of one versus the other fluid type as a function of At , θ , z_n^* and N .

6. QUANTITATIVE ANALYSIS

With reference to the definitions of Section 3 and the experiments indicated in **Figures 5** and **7**, **Figure 8** shows the evolution of A_j^* and B_j^* for different N . **Figures 8a, b** respectively show the time variation of dispersed (**Eq. 8**) and bulk area (**Eq. 7**). As anticipated, A_{disp}^* increases with time, however, the curves in





question exhibit smaller slopes for larger $\mathcal{N}$: the dispersed phase is fed by the bulk phase, so any increase in bulk fluid drainage results in a corresponding decrease in the volume of the dispersed phase. Focusing on **Figure 8 b**, it is evident that A_{bulk}^* exhibits an even greater sensitivity to $\mathcal{N}$ than does A_{disp}^* . Notably, for experiments with $\mathcal{N} = 8$ or 10 , A_{bulk}^* plateaus just above 0.2 .

From the equations of Section 3, we anticipate that B_{disp}^* should be substantially less than A_{disp}^* ; a comparison of **Figures 8 a** and **c** confirms this expectation. The corresponding difference between B_{bulk}^* (**Fig. 8 d**) and A_{bulk}^* (**Fig. 8 b**) is less extreme because, by definition, bulk fluid has a density much closer to that of the source. In **Figures 8 b** and **d**, we observe that the baseline $\mathcal{N} = 0$ case represents an outlier where, for example, both A_{bulk}^* and B_{bulk}^* increase rapidly and linearly. By contrast, B_{bulk}^* and B_{disp}^* exhibit anemic growth for large $\mathcal{N}$ in which case B_{bulk}^* plateaus just as with A_{bulk}^* .

In this last paragraph, qualitative comparisons are drawn between B_{disp}^* and B_{bulk}^* . The discussion can be made more precise by considering $\bar{B}_{\text{disp}}^*$. According to **Equation 13**, $\bar{B}_{\text{disp}}^*$ measures the buoyancy of the dispersed phase as a fraction of the overall buoyancy associated with the gravity current. **Figure 9** shows $\bar{B}_{\text{disp}}^*$ versus time and $\mathcal{N}$. Here it is apparent that $\bar{B}_{\text{disp}}^*$ generally increases as the number of open fissure holes is increased. As regards the influence of t^* , the dependence is more nuanced: for $\mathcal{N} \geq 2$, we observe a modest increase of $\bar{B}_{\text{disp}}^*$ with t^* but the trend is reversed when drainage is eliminated such that $\mathcal{N} = 0$. Note, however, that estimates of $\bar{B}_{\text{disp}}^*$ for $\mathcal{N} = 0$ and small t^* may suffer from a bias owing to the elimination, by cropping, of the region directly adjacent to the nozzle. In said region, most of the fluid discharged by the nozzle is expected to be of the bulk phase variety owing to the limited opportunity

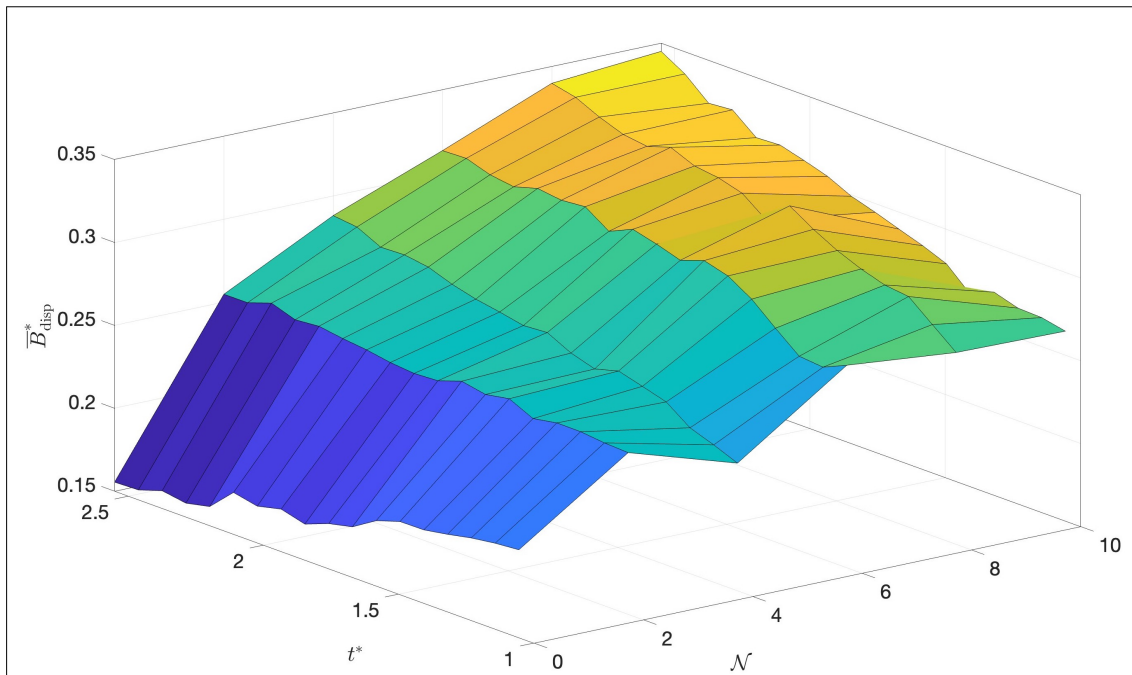


Figure 9: Dispersed buoyancy fraction versus time and $\mathcal{N}$. Here we consider the same set of experiments from **Figures 5, 7, and 8**.

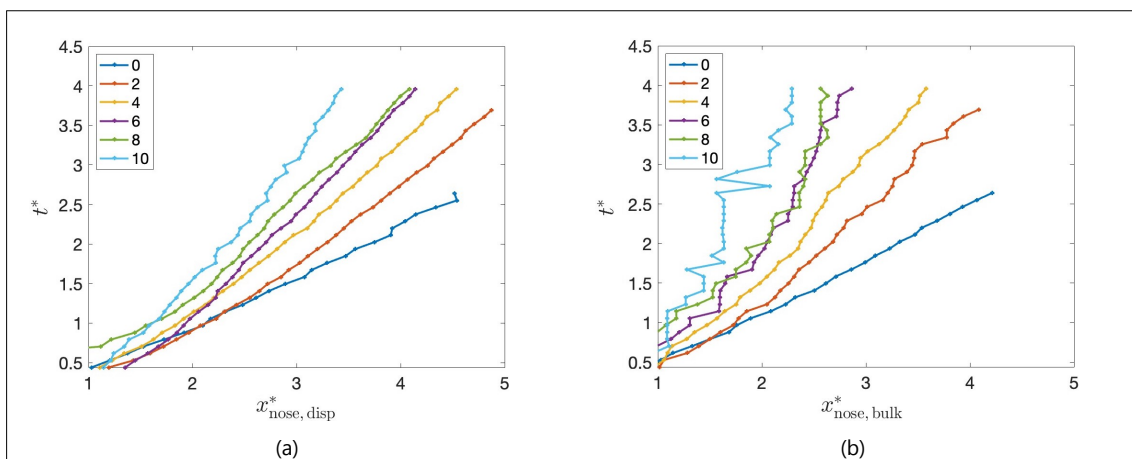
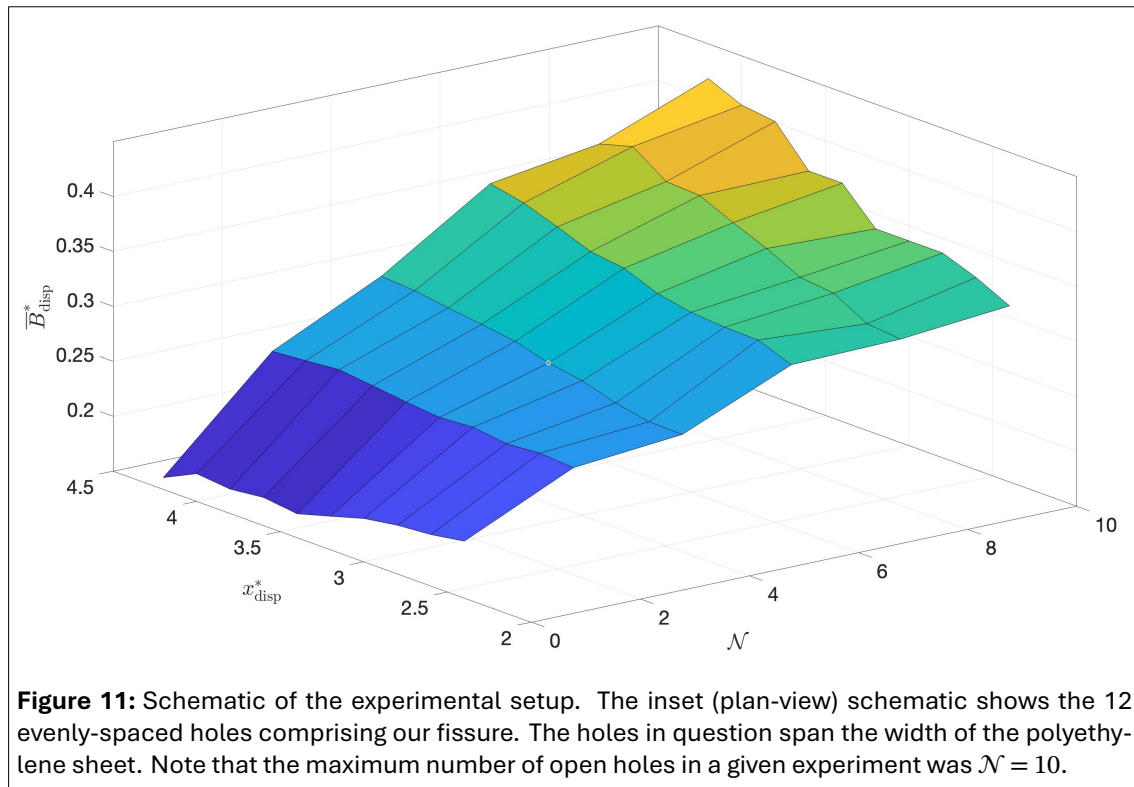


Figure 10: Time evolution of the gravity current front as characterized by the **(a)** dispersed phase, $x_{nose, disp}^*$ and **(b)** bulk phase, $x_{nose, bulk}^*$. Here we consider the same set of experiments from **Figures 5, 7, 8 and 9**. The greater scatter observed in **(b)** for large $\mathcal{N}$ is a consequence of the gravity current becoming very thin and therefore harder to visualize in experimental images -- see e.g. **Figure 7**.

for mixing with the ambient. By discounting this amount of bulk fluid, it may be the case that estimates of $\bar{B}_{disp}^*$ moderately over-predict the true value of the dispersed buoyancy fraction. As such, we propose a more robust way of characterizing the variation of $\bar{B}_{disp}^*$ below – see e.g. **Figure 11** and the discussion thereof.

Unfortunately, knowledge of the time evolution of B_j^* and even A_j^* does not provide especially meaningful insights into the rate of frontal advance of the gravity current, whether this is measured with respect to the bulk or dispersed phases. For this reason, and with reference to the same canonical set of experiments considered in **Figures 5, 7, 8, and 9**, **Figure 10** shows time-series plots of the gravity current nose positions. After an initial adjustment phase, $x_{nose, disp}^*$ shows a roughly linear variation with time where the front speed decreases with increasing $\mathcal{N}$: as noted above, dispersion is fed by bulk fluid, which is disproportionately impacted by drainage. Consequently, when the amount of drainage increases, it becomes

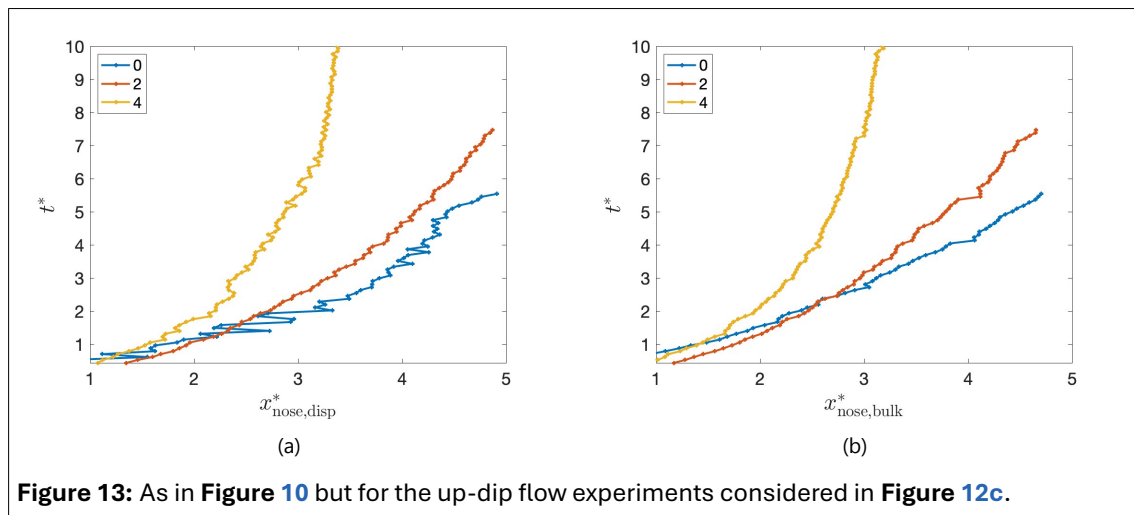
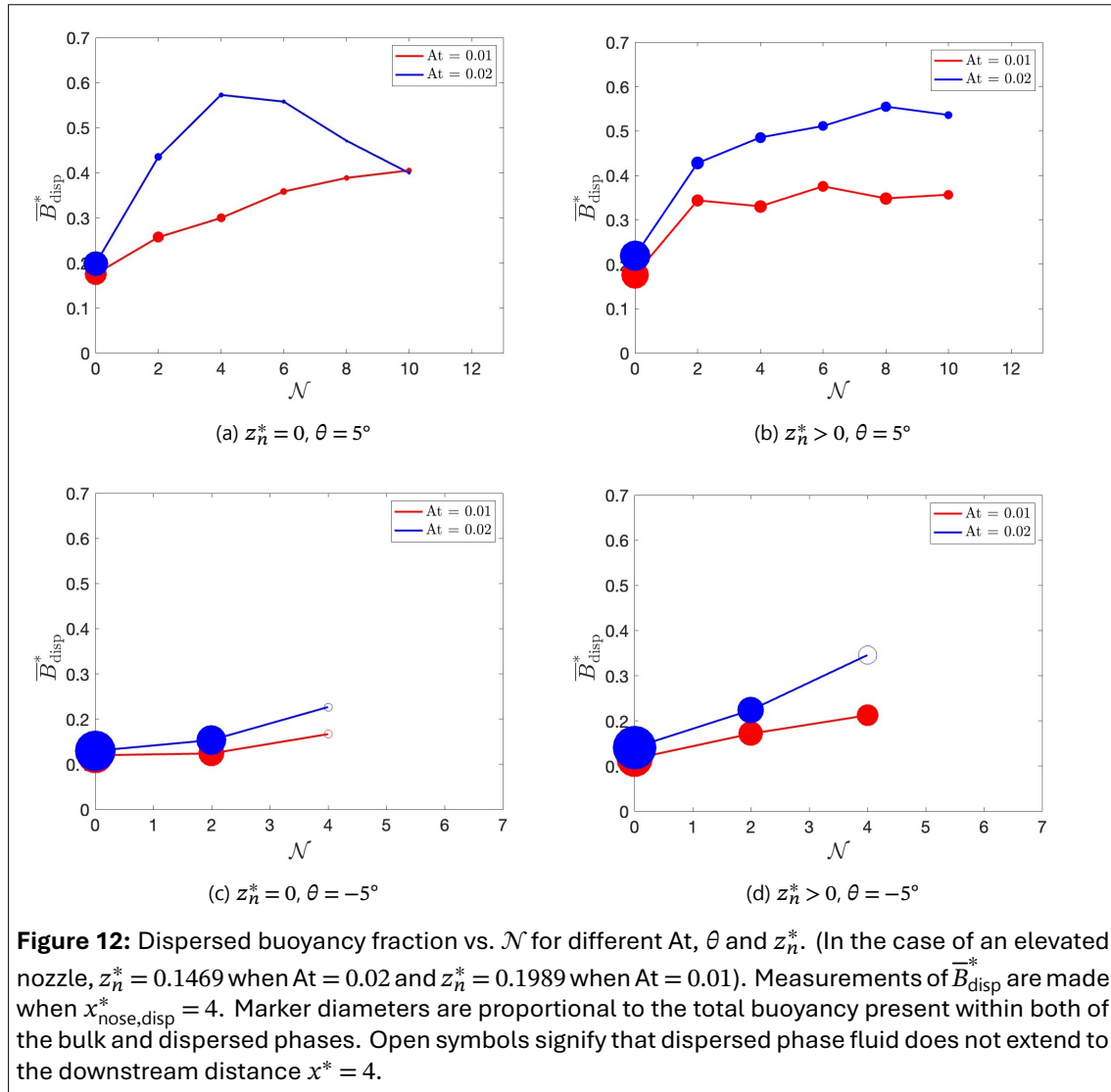


impossible for $x_{nose, disp}^*$ (or $x_{nose, bulk}^*$) to advance too quickly in the downstream direction. Indeed, the bulk phase data depicted in **Figure 10b** exhibit a greater sensitivity to $\mathcal{N}$ as evidenced by the fact that the associated time-series curves form a wider fan than is observed for the dispersed phase data of **Figure 10a**. When $\mathcal{N} = 8$ or 10 and t^* is large, the bulk phase is nearly arrested altogether. In these cases in particular, it seems doubtful that $x_{nose, bulk}^*$ will ever reach $x^* = 3$.

The results of **Figures 10a,b** suggest a different way of tracking the flow evolution of a particular experiment: rather than measuring e.g. $\bar{B}_{disp}^*$ against t^* , we can instead track the change of $\bar{B}_{disp}^*$ as $x_{nose, disp}^*$ reaches a fixed sequence of values. Such is the philosophy of **Figure 11**, which replots the data of **Figure 9** but with the horizontal axis t^* replaced by $x_{nose, disp}^*$. In contrast to **Figure 9**, the variation of $\bar{B}_{disp}^*$ is smoother than before. Partly, this is an artifact of the coarser resolution applied in **Figure 11**. However, the regularization of the surface for small values of $\mathcal{N}$ in particular suggests that frontal location rather than time may be the more meaningful metric when measuring the gravity current evolution. In any event, **Figure 11** reaffirms that $\bar{B}_{disp}^*$ changes only by a moderate amount over the course of a typical experiment but that the dependence of $\bar{B}_{disp}^*$ on $\mathcal{N}$ is more sensitive. Given this insight, we now consider the influence of other parameters, which we have deliberately held fixed in **Figures 5, 7, 8, 9, 10** and **11**.

Figure 12 shows $\bar{B}_{disp}^*$ versus $\mathcal{N}$ for two different values of At and θ where the left- and right-hand side panels respectively consider $z_n^* = 0$ and $z_n^* > 0$. The top panels assume $\theta = 5^\circ$ such that gravity current fluid flows down-dip whereas bottom panels assume $\theta = -5^\circ$ such that gravity current fluid flows up-dip. Although all four panels of **Figure 12** consider the dispersed buoyancy fraction as the y-axis variable, marker sizes provide an indication of the total buoyancy present in both the bulk and dispersed phases. As expected, the markers having the largest diameters are therefore observed for the smallest $\mathcal{N}$, $\mathcal{N} = 0$ corresponding to the case of no fissure drainage.

The red curve of **Figure 12a** revisits the data from the back left edge of the surface from **Figure 11**; accordingly, we observe a monotone increasing relationship between $\bar{B}_{disp}^*$ and $\mathcal{N}$. Doubling the value of At , i.e. shifting from the red curve to the blue curve has two important consequences. Firstly, and except at the limits $\mathcal{N} = 0$ or 10 , the dispersed buoyancy fraction is notably larger for $At = 0.02$ than it is for $At = 0.01$: a larger At is associated with larger gravity current densities and therefore larger drainage velocities. In



turn, more bulk fluid drains through the fissure when $At = 0.02$, which has the effect of increasing $\bar{B}_{disp}^*$. Secondly, the blue curve exhibits an intriguing non-monotone variation with the number of open fissure holes such that $\bar{B}_{disp}^*$ decreases with $\mathcal{N}$ for $\mathcal{N} \gtrsim 5$. As can be inferred from **Figure 6**, and for sufficiently large $\mathcal{N}$ and At , fissure drainage becomes so robust as to include not just bulk fluid, but also dispersed fluid. The onset of such a state corresponds to a peak in the measured value of $\bar{B}_{disp}^*$.

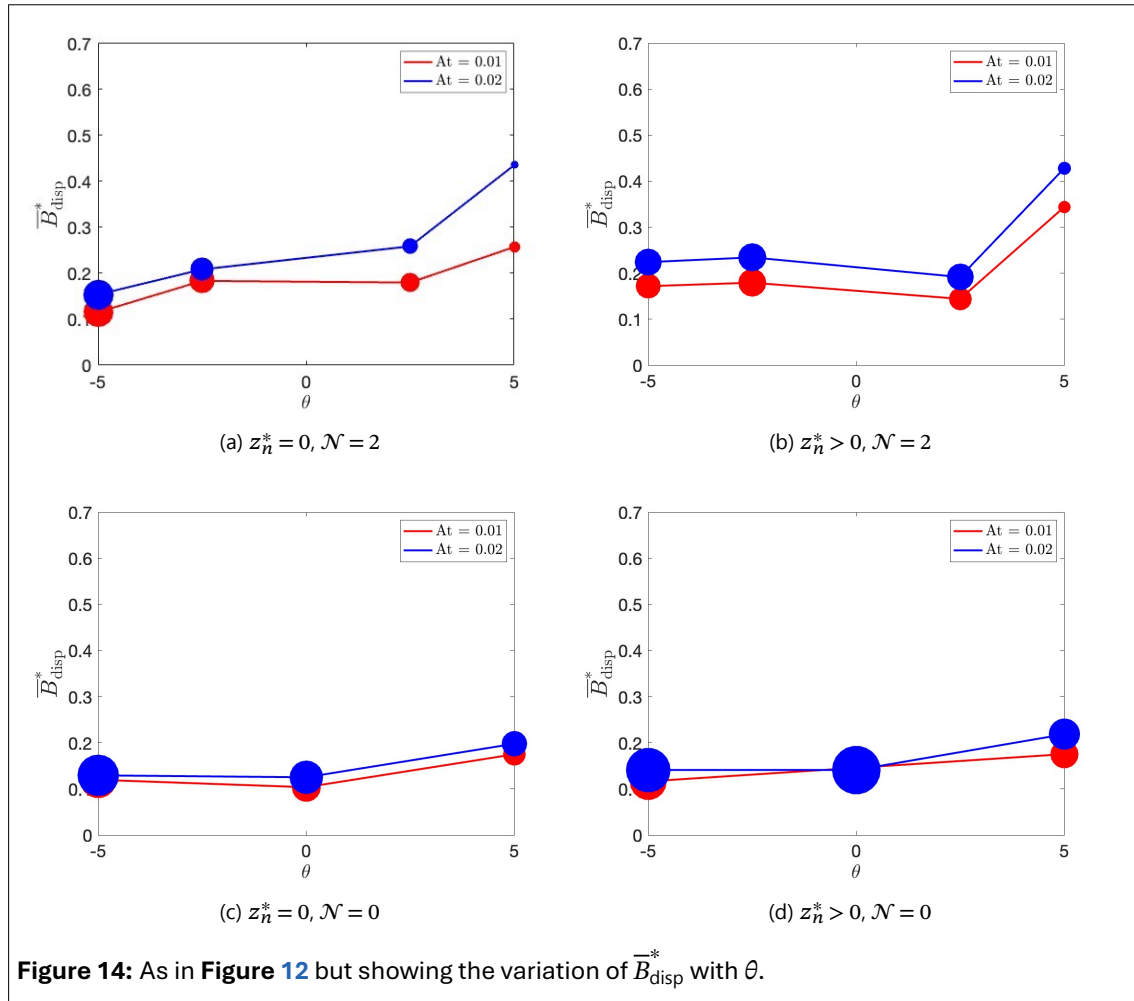


Figure 12b considers the same parameters as **Figure 12a**, but with an upward shift of nozzle elevation. The larger markers evident in **Figure 12b** versus **12a** suggest that fissure drainage is negatively impacted by raising the source and thereby diluting the dense fluid comprising the gravity current. Such dilution is a consequence of the entrainment of ambient fluid as source fluid forms a descending plume below the nozzle (23). Thus, plume entrainment exerts a nuanced influence on the dispersed buoyancy fraction. On the one hand, plume entrainment, and its concomitant decrease of the drainage velocity, results in less bulk fluid loss through the fissure, which would otherwise decrease $\bar{B}_{disp}^*$. On the other hand, the mixing associated with plume entrainment yields an immediate supply of dispersed fluid, whose appearance and subsequent down-dip propagation would otherwise increase $\bar{B}_{disp}^*$. The precise impact of these counterbalancing effects is best appreciated by comparing the red and blue curves of **Figures 12a** and **12b**. When $At = 0.01$ and the nozzle is elevated, we observe that $\bar{B}_{disp}^*$ does not steadily increase but rather saturates at approximately 0.35 for $\mathcal{N} > 2$. By contrast, and for $At = 0.02$, a raised nozzle causes $\bar{B}_{disp}^*$ to achieve its maximum value (of approximately 0.55) when $\mathcal{N} = 8$, twice the critical $\mathcal{N}$ value associated with a non-raised nozzle.

Figures 12c and **12d** present data analogous to **Figures 12a** and **12b** but for a different inclination angle, namely $\theta = -5^\circ$. Here again, $\bar{B}_{disp}^*$ generally increases with $\mathcal{N}$, albeit less aggressively than for down-dip flow. Correspondingly, $\bar{B}_{disp}^*$ values for the $\theta = -5^\circ$ cases are non-trivially smaller than those corresponding to $\theta = 5^\circ$. By contrast, the time for flow and therefore total buoyancy retained in the porous medium is much larger when the gravity current flows up-dip – compare, for example, the marker diameters when $\mathcal{N} = 2$ in **Figures 12c** and **12d** versus **Figures 12a** and **12b**. Also noteworthy is the difference of marker size when $\mathcal{N} = 4$ between **Figures 12c** and **12d**. This comparison confirms that much more buoyancy is retained in the porous medium when the nozzle is elevated, presumably because the

Table 1: Dispersed buoyancy fractions as extracted from **Figures 14 a** and **c**, where $z_n^* = 0$. For comparison, the theoretical estimate derived from the model of **Appendix B** in the **Supplementary Material** ([available online](#)) is also included. The percentage error is calculated via $(\bar{B}_{\text{disp,expt}}^* - \bar{B}_{\text{disp,thy}}^*) / [\frac{1}{2}(\bar{B}_{\text{disp,expt}}^* + \bar{B}_{\text{disp,thy}}^*)]$.

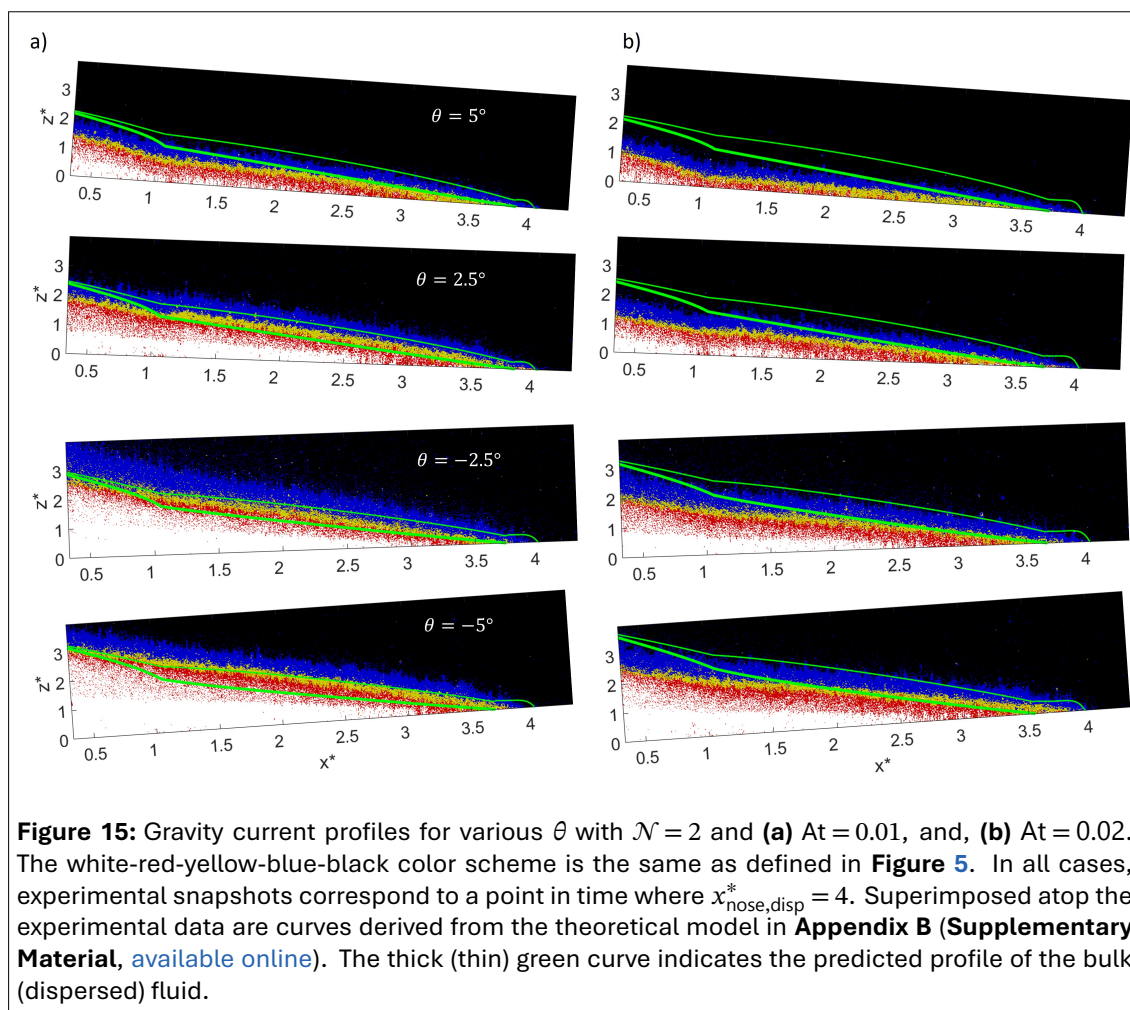
At	$\mathcal{N}$	θ (°)	$\bar{B}_{\text{disp,thy}}^*$	$\bar{B}_{\text{disp,expt}}^*$	% error
0.01	0	−5	0.101	0.120	17.2
		0	0.122	0.104	−15.9
		5	0.149	0.175	16.0
	2	−5	0.171	0.115	−39.2
		−2.5	0.189	0.183	−3.2
		2.5	0.203	0.180	−12.0
		5	0.221	0.257	15.1
0.02	0	−5	0.126	0.135	6.9
		0	0.164	0.130	−23.1
		5	0.206	0.198	−4.0
	2	−5	0.189	0.154	−20.4
		−2.5	0.213	0.208	−2.4
		2.5	0.257	0.258	0.4
		5	0.286	0.435	41.3

plume entrainment that accompanies the raised source depresses drainage velocities. This has the effect of decreasing the volume of dense fluid discharged through the fissure, especially for larger $\mathcal{N}$.

Of course, increasing $\mathcal{N}$ carries the possibility that even the dispersed front will become arrested before reaching the downstream location $x^* = 4$. Such cases are illustrated in **Figures 12c** and **12d** by the open symbols. So as to gain additional insights into the flow evolution for these experiments (plus their smaller $\mathcal{N}$ counterparts), we show in **Figure 13** the dispersed ($x_{\text{nose,disp}}^*$) and bulk ($x_{\text{nose,bulk}}^*$) nose positions versus time. In all cases, $\text{At} = 0.01$. The yellow curves illustrate the $\mathcal{N} = 4$ case; as expected, the forward advance of both the dispersed and bulk fronts slows significantly as t^* increases. A less dramatic deceleration is noted when $\mathcal{N} = 2$ (orange curves) or, more especially, $\mathcal{N} = 0$ (blue curves). In these two cases, in particular, the dispersed layer remains comparatively thin.

Because **Figure 12** considers only two possible values for θ , i.e. $\theta = -5^\circ$ (up-dip flow) and $\theta = 5^\circ$ (down-dip flow), it is difficult to infer the precise impact of the inclination angle on $\bar{B}_{\text{disp}}^*$. Accordingly, each of the subplots of **Figure 14** fixes the values of $\mathcal{N}$ and the dimensional nozzle elevation, but considers a more complete range of θ . Consistent with our previous remarks, $\bar{B}_{\text{disp}}^*$ generally increases with θ , however, **Figures 14a** and **14b** confirm that the variation can be decidedly nonlinear. These subplots further reveal that, as the inclination angle varies from $\theta = -5^\circ$ to $\theta = 5^\circ$ there is a corresponding decrease of marker size: when $\theta = 5^\circ$ such that the gravity current flows down-dip, advection speeds are large and the dispersed front reaches the downstream position $x^* = 4$ in much less time than is required when $\theta = -5^\circ$. Thus, there is much more opportunity for dense fluid to accumulate in the porous medium when the gravity current flows up-dip. This same trend is likewise evident when $\mathcal{N} = 0$ (bottom row of **Fig. 14**), although the decrease of marker size is less dramatic. In a similar spirit, the increase of $\bar{B}_{\text{disp}}^*$ as θ increases from -5° to 5° is comparatively minor: without draining and the disproportionate removal of bulk fluid, the fraction of bulk to dispersed fluid varies little with θ or, for that matter, At .

Taken together, **Figures 12** and **14** show that making adjustments to $\mathcal{N}$ and θ can cause $\bar{B}_{\text{disp}}^*$ to vary by almost half an order or magnitude. Though obviously nontrivial, this variety must be weighed against the much more substantial mixing that is possible in hetero- versus homogeneous porous media. For instance, Sahu & Neufeld (24) performed experiments that explored gravity current flow through a porous medium characterized by discrete layers of different permeability. Using as their mixing metric the effective dispersive entrainment coefficient, they concluded that “the amount of mixing in a heterogeneous medium can be higher by several orders of magnitude than that in a homogeneous medium depend-



ing on the type of heterogeneity." This substantial increase of mixing efficiency follows from the kind of motion observed by Sahu & Neufeld (24), i.e. their gravity currents first elongated through a layer of high permeability then experienced distributed drainage into a layer of low permeability. The resulting formation and elongation of convective fingers resulted in considerable mixing with the ambient fluid. In turn, the gravity current developed a blunt nose and lost its long, thin shape. By contrast, **Figure 5** and **Figure 6** for instance confirm that the gravity currents of interest here become more, not less, slender over time. More importantly, we downplay the mixing directly associated with (discrete) basal draining focusing instead on the mixing that occurs along the upper (i.e. density-stable) surface of the gravity current. In this way, our results are, when inverted and extrapolated to real geophysical flows, reminiscent of buoyancy-driven flow along the underside of a caprock that is tight except for the appearance of a limited number of individual fissures.

7. COMPARISON WITH THE THEORY OF SHEIKHI ET AL.

The comparisons drawn in **Figures 14 a** and **c** can be extended in another direction, i.e. by contrasting measured results with fitted predictions derived from the theoretical model of Sheikhi et al. (27). (A brief summary of Sheikhi et al.'s model appears in **Appendix B (Supplementary Material, available online)**. Because the model in question does not allow for non-zero z_n^* , no comparisons are possible with the data of **Figures 14 b** and **d**.)

Theoretical estimates for $\bar{B}_{\text{disp}}^*$ are presented in **Table 1**. Also included in this table are the experimental data from **Figures 14 a,c** organized by At , $\mathcal{N}$ and θ . The error estimates that appear in the final column of **Table 1** quantify the difference between theoretical and experimental estimates of $\bar{B}_{\text{disp}}^*$ and include a

roughly equal proportion of positive and negative values. Complementing the above discussion, **Figure 15** shows experimental snapshots from the $\mathcal{N} = 2$ experiments of **Table 1** where, in each case, $x_{\text{nose,disp}}^* = 4$. Panels **(a)** and **(b)** respectively consider $At = 0.01$ and $At = 0.02$ and the inclination angle is as indicated. In each sub-figure, we return to the white-red-yellow-blue-black color scheme adopted in **Figures 5, 6** and **7**. Superimposed on the experimental snapshots are solid curves showing the theoretically-predicted profile for the bulk fluid (thick green curve) and the dispersed fluid (thin green curve). Ideal agreement would position the thick green curve along the red-yellow boundary and the thin green curves along the blue-black boundary and, indeed, such overlap is nearly realized in select cases e.g. $At = 0.01$, $\theta = 2.5^\circ$, $x^* \gtrsim 1$ or $At = 0.02$, $\theta = -5^\circ$, $x^* \gtrsim 1.5$. Elsewhere, greater discrepancies are observed, most especially when $At = 0.02$ and $\theta = 5^\circ$.

Taken together, **Table 1** and **Figure 15** suggest that the theoretical model developed in Sheikhi et al. (27) does only a fair job of predicting experimental trends. Consider, for example, the case $At = 0.01$, $\mathcal{N} = 2$ and $\theta = 2.5^\circ$. **Figure 15 a(ii)** shows arguably the best agreement between theory and experiment of any of the panels for the figure in question. Even so, there is a -12.0% error between $\bar{B}_{\text{disp,thy}}^*$ and $\bar{B}_{\text{disp,expt}}^*$. By contrast, when $At = 0.02$, $\mathcal{N} = 2$ and $\theta = 2.5^\circ$, $\bar{B}_{\text{disp,thy}}^*$ and $\bar{B}_{\text{disp,expt}}^*$ are in near perfect agreement and yet **Figure 15 b(ii)** indicates that both the thick and thin green curves overestimate their respective boundaries. The observation concerning $At = 0.01$, $\mathcal{N} = 2$ and $\theta = 2.5^\circ$ suggests that the theoretical model may over-estimate the degree the mixing by dispersion. Additional studies are recommended to determine whether the linear entrainment relationship developed in Sheikhi et al. (27), and adapted from investigations of analog non-porous media flows, requires refinement. Meanwhile, the observation concerning $At = 0.02$, $\mathcal{N} = 2$ and $\theta = 2.5^\circ$ suggests that the degree of fissure drainage may be insufficient, especially for higher gravity current densities. This implies that the fissure draining law quantified by **Equation B8** in **Appendix B (Supplementary Material, available online)**, and derived from a generalization of Bernoulli's principle, may require modification for sufficiently large values of c_s .

A further persistent challenge for the theoretical model is to predict the correct profile heights upstream of the fissure at $x^* = 1$. This latter observation suggests that the theoretical model should be modified to allow for more dispersive mixing in the neighborhood of the gravity current source. The model presently requires the thick and thin green curves to merge in the limit $x^* \rightarrow 0$ but such an assumption is evidently not supported by the available experimental data.

8. CONCLUSIONS

Whereas dispersive mixing in porous media has attracted a great deal of attention, relatively few studies have explored dispersive mixing in the specific context of gravity current flow. Of particular interest is to couple dispersion and gravity current mass loss due to drainage. The current (experimental) work restricts drainage to an isolated fissure and therefore preserves the long and thin character of the gravity current. Doing so, and likewise examining a baseline case where the isolated fissure is closed altogether, allows us to correlate drainage and dispersion and to explore the relationship between these two variables by leveraging the image processing algorithm described in Section 4. Laboratory experiments are performed over a range of source densities (At), inclination angles (θ), fissure geometries ($\mathcal{N}$) and source elevations (z_n) and consider as a key metric the dispersed buoyancy fraction defined by **Equation 13**. The dispersed buoyancy fraction measures the fraction of total buoyancy that resides in the dispersed phase and so serves as an effective measure of the degree of mixing between the gravity current and ambient.

Based on our experimental measurements, the following key findings emerge:

- As fissure draining becomes more significant, so too does the relative importance of dispersion: draining preferentially removes so-called bulk fluid having a density close to that of the gravity current source, ρ_s . Thus, in comparative sense, the domain typically contains more dispersed fluid, whose density falls closer to the ambient density, $\rho_a < \rho_s$.

- The effect just described becomes more prevalent at larger ρ_s (i.e. larger At) because of the corresponding increase of the drainage velocity. Generally similar comments apply to the number, $\mathcal{N}$, of discrete openings comprising the isolated fissure. Indeed, for sufficiently large $\mathcal{N}$, we find that the gravity current becomes arrested such that its volume and buoyancy both plateau.
- When the (dense) gravity current is fed by an elevated source such that a descending plume forms, the amount of dispersive mixing experienced upstream of the fissure increases. As a consequence, however, fissure drainage is depressed. Thus, the dispersed buoyancy fraction or $\bar{B}_{\text{disp}}^*$ tends to an asymptotic value in the limit of large $\mathcal{N}$ – see e.g. **Figure 12 b**.
- Forcing the gravity current to propagate up-dip causes the flow to arrest earlier and even causes the dispersed phase to reach a terminal “run-out” length. Because of the limited opportunity for dispersive mixing when the up-dip inclination angle is sufficiently large, the volume of dispersed fluid realized for large negative θ is much smaller than what is realized for large positive θ . On the other hand, for $\theta = -2.5^\circ$, $\theta = 0^\circ$ and even $\theta = 2.5^\circ$, **Figure 14** confirms that the degree of dispersion is often comparable to that measured at $\theta = -5^\circ$.

Although we have avoided extrapolating our results to real UHS systems, which present many more complications than are considered in our idealized experiments, it is worth considering the significance of this last finding. In particular, provided structural trapping in the form of an anticline is available, the degree of dispersion is predicted to be approximately independent of dip angle. Of course, more steeply-sloped anticlines may offer other advantages relative to their shallow-sloped counterparts e.g. hydrogen will ultimately collect in a deeper layer such that, during the production phase, the likelihood of coning (i.e. the co-extraction of hydrogen and cushion gas) is minimized.

In drawing comparisons between measured results and the analog theory previously published by Sheikhi et al. (27), **Table 1** shows fair agreement between experimental and theoretical estimates of $\bar{B}_{\text{disp}}^*$. The ability of the theory to correctly anticipate the gravity current profile (including the shape of the bulk and dispersed phases) is likewise nuanced as **Figure 15** confirms. Whereas generally good agreement is seen at large x^* and small At and θ , the model significantly over-predicts the height of both phases when At and θ are large. One possible contributor to this discrepancy is that the model assumes very limited mixing in the neighborhood of the source, an assumption that ought to be relaxed in further iterations of the theory.

Other ideas for future work include adding multiple isolated fissures or including some degree of heterogeneity within the porous medium itself. Whereas the experiments in question could be performed by a straightforward modification of the set-up of Section 2.1, there remain other important topics for investigation that would necessitate a more elaborate experimental redesign. For instance, the flows we consider are nominally 2-D rectilinear. However, given that the motivation for this study derives from the seasonal storage of hydrogen in depleted natural gas reservoirs, it would be helpful to consider more complicated flow patterns e.g. 2-D axisymmetric or fully 3-D. In this latter case, in particular, it would be important to characterize the role of dispersion in the transverse direction. By design, transverse dispersion is ignored here, however, its impact at the large spatial scales that characterize real UHS flows is, almost certainly, important. By extension, we do not expect the results of e.g. **Figure 14** to be quantitatively accurate when transverse dispersion results in significant (i.e. non-local) variations in the pattern of gravity current spread.

Also critical to explore in the UHS context is the impact of a transient source that discharges, then later aspirates, gravity current fluid having a different density and viscosity than the fluid saturating the porous medium. For such a scenario, the evolution of the gravity current and, more especially, the dispersed phase, has yet to be fully characterized. Such a characterization is essential to an evaluation of the feasibility, commercial and otherwise, of field-scale hydrogen storage projects.

STATEMENTS AND DECLARATIONS

Supplementary Material

Supplementary material for this paper is available at <https://doi.org/10.69631/b5x6xn52>, and includes a detailed summary of all laboratory experiments conducted in this study, along with a brief review of the derivation of the theoretical model originally presented in Sheikhi et al. (27).

Author Contributions

M. Singh performed the experiments and post-processed the experimental images, with detailed technical assistance from K.S. Bharath. S. Sheikh developed the theoretical model and generated the theoretical data that appears, for example, in **Table 1**. M.R. Flynn supervised the work and co-wrote the manuscript with M. Singh.

Conflicts of Interest

All four authors declare that they have no conflict of interest.

Data, Code & Protocol Availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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