








UNDERSTANDING FRACTURE APERTURE AND PERMEABILITY EVOLUTION DUE TO CARBONATE MINERALIZATION UTILIZING 3D PRINTING

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1. METHODOLOGY FOR CALCULATING SURFACE ROUGHNESS PARAMETER

For quantitative comparison, the following surface roughness parameters were utilized which are in accordance with ISO 25718-6 (2) and ASME B46.1 (1).

S_a , *Areal average surface roughness*: The arithmetic average of the absolute values of the profile height deviations recorded within the evaluation length or evaluation area and measured from the mean line. Analytically S_a can be calculated using the following equation (Eq. S1) where N and M represent the number of array sizes in the evaluation direction.

$$S_a = \frac{1}{MN} \sum_{k=1}^M \sum_{j=1}^N |Z_{jk}| \quad (S1)$$

S_{sk} , *Skewness*: Skewness is the quotient of the mean cube value of $Z(x)$ and the cube of the root means square roughness or ($S_q = \sqrt{\frac{1}{MN} \sum_{k=1}^M \sum_{j=1}^N |Z_{jk}^2|}$) within a sampling length. If $S_{sk} = 0$, symmetric against the mean line (e.g. normal distribution). If $S_{sk} > 0$, the deviation is beneath the mean line, or else if $S_{sk} < 0$, the deviation is above the mean line. A negative skewness means the surface has more valley depths than peak heights (Eq. S2).

$$S_{sk} = \frac{1}{(S_q)^3} \frac{1}{MN} \sum_{k=1}^M \sum_{j=1}^N |Z_{jk}^3| \quad (S2)$$



S_{ku} , *Kurtosis*: The quotient of the mean quartic value of $Z(x)$ and the fourth power of S_q within a sampling length. In other words, if $S_{ku} = 3$, it is similar to a normal distribution, if $S_{ku} > 3$ the height distribution is sharp, and if $S_{ku} < 3$ the height distribution is flatter (Eq. S3).

$$S_{ku} = \frac{1}{(S_q)^4} \frac{1}{MN} \sum_{k=1}^M \sum_{j=1}^N |Z_{jk}^4| \quad (S3)$$

S_{dr} , *Developed interfacial area ratio*: The developed interfacial area ratio is categorized as surface texture parameters. It quantifies how much surface area in a particular region of interest contributes to the texture compared to a nominally flat surface. Basically, it is the percentage of surface area that the surface texture adds to an ideal smooth and flat surface of the same cross-sectional area as the measurement region (Eq. S4).

$$S_{dr} = \frac{(\text{Surface area with texture}) - (\text{Ideally smooth surface area})}{(\text{Ideally smooth surface area})} \quad (S4)$$

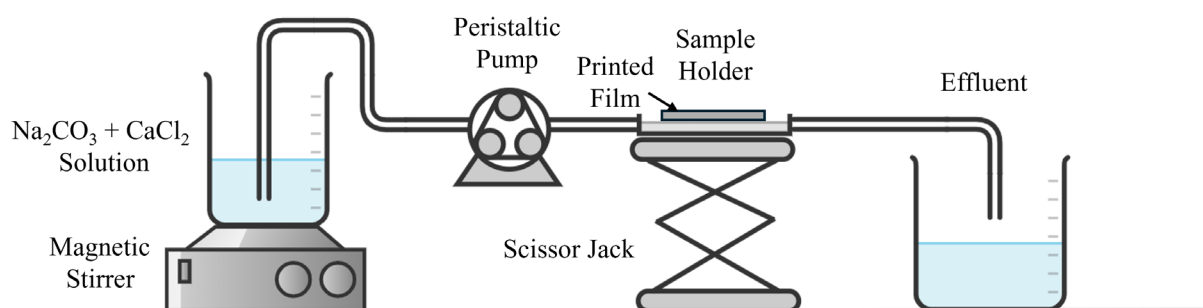


Figure S1: Experimental setup for 2D film calcite precipitation.

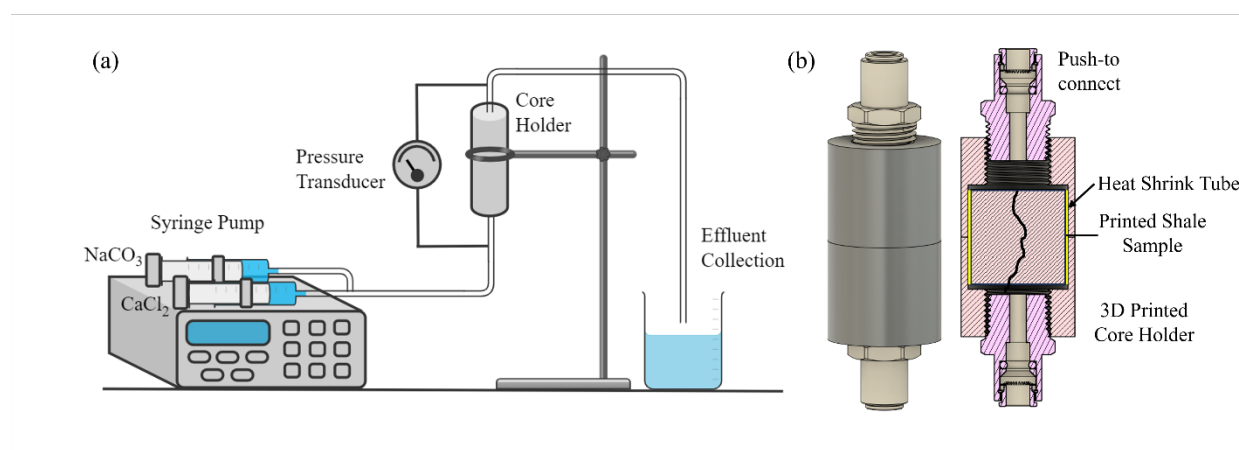


Figure S2: (a) Experimental setup for plug flow column calcite precipitation experiment, (b) 3D printed core holder and the cross-section.

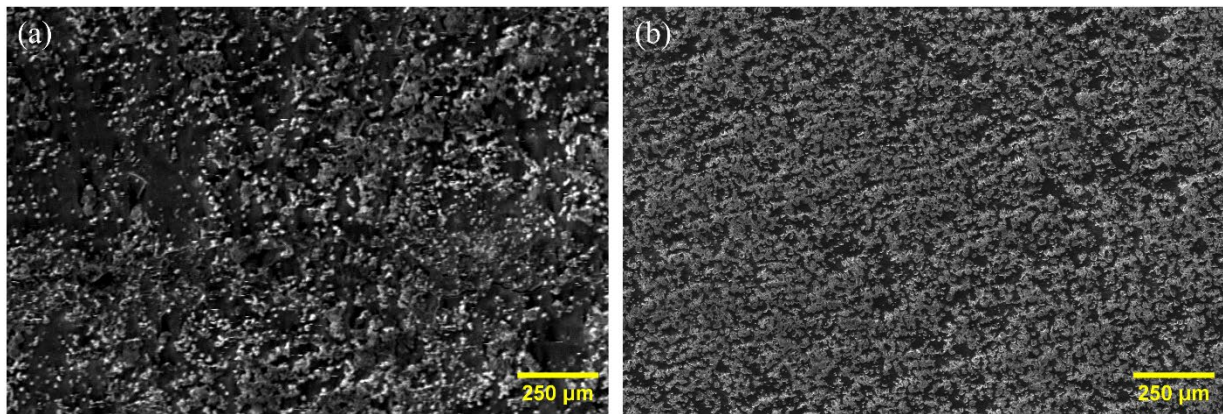


Figure S3: SEM image of calcite precipitation on DLP fabricated 2D films after **(a)** 4-hour flow experiment and **(b)** 24-hour flow experiment.

References

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2. ISO 25178-6:2010. *Geometrical Product Specifications (GPS) — Surface Texture: Areal. Part 6: Classification of Methods for Measuring Surface Texture*. (2010). <https://www.iso.org/standard/42896.html>